Design, Modeling and Control of a Top-loading Fully-Actuated Cargo Transportation Multirotor

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Abstract—Existing multirotor-based cargo transportation does not maintain a constant cargo attitude due to underactuation; however, fragile payloads may require a consistent posture. The conventional method is also cumbersome when loading cargo, and the size of the cargo to be loaded is limited. To overcome these issues, we propose a new fully-actuated multirotor unmanned aerial vehicle platform capable of translational motion while maintaining a constant attitude. Our newly developed platform has a cubic exterior and can freely place cargo at any point on the flat top surface. However, the center-of-mass (CoM) position changes when cargo is loaded, leading to undesired attitudinal motion due to unwanted torque generation. To address this problem, we introduce a new model-free center-of-mass position estimation method named as the MOCE (Model-free Online Center-of-mass Estimation) algorithm, which is inspired by the extremum-seeking control (ESC) technique. Experimental results are presented to validate the performance of the proposed estimation method, effectively estimating the CoM position and showing satisfactory constant-attitude flight performance. A video can be found at https://youtu.be/g5yMb22a8Jo

Index Terms—Unmanned aerial vehicles, extremum-seeking control, fully-actuated multirotor UAV, center-of-mass position estimation, aerial robot.

I. INTRODUCTION

M ULTIROTOR unmanned aerial vehicles (UAVs) are evolving beyond simple photography/reconnaissance platforms into logistics platforms [1], [2]. However, there are several issues with the flight and cargo loading methods of the current platform design. For instance, multirotor UAVs have limited control capabilities compared to their range of motion, which is known as "underactuation". As a result, their attitude continuously changes during flight and depends on their desired translational motion. This also causes any cargo mounted on the platform to experience rapid and constant changes in attitude during flight, which may lead to potential cargo damage. Additionally, the commonly used existing method of

Manuscript received: January, 17, 2023; Revised May, 15, 2023; Accepted July, 9, 2023.

This paper was recommended for publication by Editor Pauline Pounds upon evaluation of the Associate Editor and Reviewers' comments.

This work was supported by the National Research Foundation of Korea grants funded by the Korea government (MSIT) (No. 2022R1F1A1075373, 2022R1A4A1032030).

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Digital Object Identifier (DOI): see top of this page.

storing cargo in a dedicated cargo hold mounted underneath the platform makes loading/unloading difficult [4], [5].

To increase the logistic utility of UAVs, developing novel flight hardware that can maintain a constant attitude and conveniently load and unload cargo is necessary. This will require the hardware to possess a feature known as "full actuation," which enables the UAV to adopt arbitrary attitudes independent of translational motion. Therefore, in this study, we introduce a new fully-actuated UAV platform design, which can freely and conveniently load various volumes of cargo on the top surface of the fuselage. We also introduce a modelfree center-of-mass (CoM) position estimation method essential for the fully actuated multirotor to maintain a constant attitude while loading cargo with unknown physical properties. Through the proposed design and controller, the platform can conveniently load/unload and transport cargo in a constant attitude throughout the flight, as if loading cargo into the compartment of a truck.

A. Related works

The keywords of this research are *fully-actuated multirotor UAV* and *center-of-mass position estimation*. However, research combining these two factors is limited; therefore, we investigated related studies on each.

1) Fully-actuated multirotor design: Much research has been conducted focusing on developing a fully-actuated multirotor platform to enhance the applicability of multirotor UAVs [6]. Platform type can be divided into two categories: fixed-tilt configurations and variable-tilt configurations.

For the fixed-tilt configurations, the thrusters are installed in fixed but various positions and directions. Translational motion can then be controlled independently of the current attitude by controlling the magnitude and direction of the sum vector of all thrusts [7]–[9]. Since the fixed-tilt configurations can create a relatively wide range of control wrenches, they can independently control translational motion while taking an extreme attitude. However, these configurations are less suitable for cargo transportation since much energy is consumed to compensate for the internal forces among thrusters.

In variable-tilt configurations, a servomechanism is added to control the thrust direction and enable additional control degrees of freedom (DOF). In [10]–[12], servo actuators with one or two DOF are installed with each propeller. However, because multi-rotor hardware has a rigid body characteristic, the minimum number of actuators required for a full DOF motion is six. If the number of hardware actuators exceeds this, the platform becomes overactuated and redundant. Since redundancies cause an unnecessary increase in weight and power consumption, some studies have achieved full actuation by adding only two servo mechanisms instead of four [13], [14].

The variable-tilt configurations allow control of each thruster's direction independently so that almost all thrust forces can be used to overcome gravity. This characteristic makes the variable-tilt configurations more suitable for cargo transportation than the fixed-tilt configurations. Also, a fullyactuated platform is preferable compared to an overactuated platform since it can maintain a constant attitude during flight while minimizing weight and energy consumption.

2) Center-of-mass position estimation: Existing studies for estimating CoM include [15]–[17]. In [15], a maximum likelihood estimation scheme is established utilizing raw inertial measurement unit (IMU) measurements and rotor speed data. The scheme is then post-processed to find accurate CoM data. Since the process is based on post-processing batch optimization systems, it is impossible to know the changing platform characteristics during flight. On the contrary, in [16] and [17], internal sensor-based online CoM estimation is introduced. However, these methods are not easily applicable in situations carrying unspecified cargo because they depend on the Kalman filter technique. This technique requires model information, including the physical property of the cargo, before the flight for guaranteed performance.

B. Contributions

In this study, we propose a new fully-actuated flight hardware design that can load unknown payloads freely on the flat upper area of the platform while maintaining a constant fuselage and cargo attitude during flight. The new design places all propulsion systems inside the fuselage, giving it the additional merit of being safe for people when flying in a populous environment. We also propose a novel technique to accurately estimate the altered CoM position of the platform after the cargo loading. Our approach, which we named the MOCE (Model-free Online Center-of-mass Estimation) algorithm, is inspired by the model-free cost optimization process known as the "extremum-seeking control (ESC)" method [18]. The new estimation algorithm modifies the conventional ESC scheme to account for the inherent flight characteristics of the newly developed platform. As a result, we can precisely estimate the CoM position, even without any physical information about the loaded cargo, thanks to the model-free nature of the ESC algorithm.

The paper is structured as follows: Section II presents the hardware design and system's kinematics and dynamics. Section III introduces the controller design for full actuation, including control allocation, MOCE algorithm, and stability analysis. Section IV shows experimental results validating the cargo transportation flight performance. Section V provides a brief summary and conclusion.

II. HARDWARE

This section introduces the design of the proposed hardware, flight principle, and the 6-DOF propulsion mechanism that



Fig. 1. Configuration diagram of the top-loading fully-actuated cargo transportation multirotor UAV. The new platform consists of two vertically intersecting arm assemblies, each equipped with a propeller at both ends. Each assembly can rotate axially through a servomechanism, enabling six degrees of freedom flight utilizing four propellers and two servomechanisms.

brings fully actuated flight performance. We also introduce the kinematics and dynamics of the proposed hardware.

A. Hardware design

Our hardware design aims to construct a propulsion mechanism that independently generates a three-dimensional torque vector for attitude control and a three-dimensional force vector for translational motion control. To achieve this goal, the novel propeller tilting mechanism is configured with a minimum number of servomechanisms while keeping the physical properties of the platform, such as the moment of inertia (MoI), constant during the thruster tilting motion. By ensuring that the moment of inertia is invariant to the servomotor control, the entire system can be analyzed as a single rigid body, thereby securing the convenience of the controller design.

Fig. 1 shows the structure of the proposed UAV. The fuselage has a cubic exterior, and all propulsion systems are housed inside the fuselage. The upper part of the fuselage has a flat surface without any protrusions, and a microstructure is installed to provide high friction between the payload and the fuselage. This design feature allows the cargo to be placed at any point on the flat top surface of the fuselage without a dedicated cargo hold. There are also many perforations on the top and side of the platform, minimizing changes in the aerodynamic characteristics of the propeller inside the fuselage. The inside of the fuselage contains a column with a single Dynamixel 2XC-430 servomotor in the center, which has two servo-controlled axes perpendicular to each other, which we refer to as 'Axis 1' and 'Axis 2'. Two drone arm assemblies are then positioned along each axis of the servomotor, where two coaxial propeller propulsion systems are positioned at both ends of each arm. The longitudinal principle axis of inertia for each assembly is designed to coincide with the axis of the servomotor; thus, the moment of inertia of the fuselage does not change even when the servomotor is in a rotating motion. Through this design, thrusters 1 and 3 in Fig. 1 can generate horizontal thrust in the body y axis direction by θ_1 angle control of the servomotor, and thrusters 2 and 4 can generate body x axis directional force by θ_2 angle control. Ultimately, the system obtains a total of 6-DOF control utilizing two servomotors and four propulsion systems.

B. Kinematics

To realize fully actuated flight, the platform should generate three-dimensional attitude control torques and translational forces independently using the six aforementioned actuators. Let ${}^{B}\mathbf{T} = [\tau_{x} \ \tau_{y} \ \tau_{z}]^{T} \in \mathbb{R}^{3\times 1}$ and ${}^{B}\mathbf{F} = [F_{x} \ F_{y} \ F_{z}]^{T} \in \mathbb{R}^{3\times 1}$ be the torque and thrust force vectors acting on the platform. ${}^{B}(*)$ denotes that the vector is in the body-fixed frame of the platform. We can then define a wrench vector ${}^{B}\mathbf{W} = [{}^{B}\mathbf{T}^{T} \ {}^{B}\mathbf{F}^{T}]^{T}$ and manipulate it to control the pose of the platform. A wrench vector ${}^{B}\mathbf{W}$ should be generated with a combination of six actuator outputs: $F_{\{1,2,3,4\}}$ (propeller thrusts) and $\theta_{\{1,2\}}$ (servo angles). Therefore, in this subsection, we examine the relationship between the actuator output and the wrench through a kinematics analysis of the hardware and use the information for deriving the control allocation method in Section III.

Based on Fig. 1, the overall moments ${}^{B}\mathbf{T}$ generated by the set of thrusters become as follows.

$${}^{B}\mathbf{T} = \sum_{i=1}^{4} \left(\left({}^{B}\mathbf{r}_{i} - {}^{B}\mathbf{p}_{c} \right)_{\times} - (-1)^{i} \xi \mathbb{I}_{3 \times 3} \right) {}^{B}\mathbf{F}_{t,i}$$
(1)

Here, ${}^{B}\mathbf{r}_{i}$ and ${}^{B}\mathbf{p}_{c} = [x_{c} \ y_{c} \ z_{c}]^{T}$ are position vectors of the *i*th thruster and the CoM position of the platform, respectively, ξ is a ratio between the yaw-steering reaction torque and the thrust force of the propeller thruster, $\mathbb{I}_{3\times3}$ is a 3×3 identity matrix, and ${}^{B}\mathbf{F}_{t,i} = [F_{t,i,x} \ F_{t,i,y} \ F_{t,i,z}]^{T}$ is the thrust force vector generated by the *i*-th thruster. $(*)_{\times}$ is a matrix form of the cross-product operation.

For ${}^{B}\mathbf{F}_{t,i}$, thrust force can be distributed in the horizontal and vertical directions through servomotor control. Based on the hardware configuration shown in Fig. 1, the thrust vector of each motor is described as follows:

$${}^{B}\mathbf{F}_{t,1} = [0 \, \sin\theta_{1} \, -\cos\theta_{1}]^{T}F_{1} \\ {}^{B}\mathbf{F}_{t,2} = [-\sin\theta_{2} \, 0 \, -\cos\theta_{2}]^{T}F_{2} \\ {}^{B}\mathbf{F}_{t,3} = [0 \, \sin\theta_{1} \, -\cos\theta_{1}]^{T}F_{3} \\ {}^{B}\mathbf{F}_{t,4} = [-\sin\theta_{2} \, 0 \, -\cos\theta_{2}]^{T}F_{4}$$
(2)

Then, the cumulative three-dimensional force vector that controls the translational motion of the platform is as follows:

$${}^{B}\mathbf{F} = \begin{bmatrix} -F_{A2}\sin\theta_{2} \\ F_{A1}\sin\theta_{1} \\ -F_{A1}\cos\theta_{1} - F_{A2}\cos\theta_{2} \end{bmatrix}, \quad (3)$$

where $F_{A1} = F_1 + F_3$ and $F_{A2} = F_2 + F_4$ are collective forces generated from Axis 1 and 2 of the platform, respectively.

C. Dynamics

As mentioned above, the proposed platform has no change in the moment of inertia in any flight scenario because the principle axis of inertia of the drone arm assembly, which is the only moving part of the structure, is designed to coincide with the servo axis during the 6-DOF driving process. Therefore, the platform can always be treated as a rigid body, and the translational and rotational motion dynamics can be modeled as follows:

$$\begin{cases} R(\mathbf{q})^B \mathbf{F} + m\mathbf{g} = m\ddot{\mathbf{X}} \\ {}^B \mathbf{T} + {}^B \mathbf{T}_s = J^B \dot{\mathbf{\Omega}} + {}^B \mathbf{\Omega} \times J^B \mathbf{\Omega} \end{cases},$$
(4)

where $R(\mathbf{q}) \in SO(3)$ is a rotation matrix from the body coordinate to the global coordinate, $\mathbf{q} = [\phi \ \theta \ \psi]^T$ is the Euler attitude of the fuselage, and $\mathbf{g} = [0 \ 0 \ g]^T$ is the gravitational acceleration represented in the global frame. m is the mass, $\ddot{\mathbf{X}} \in \mathbb{R}^{3 \times 1}$ is the global acceleration vector, ${}^B \mathbf{T}_s$ is the reaction torque from the 2XC-430 servomotor which is negligible compared to the magnitude of ${}^B \mathbf{T}$, $J \in \mathbb{R}^{3 \times 3}$ is the moment of inertia tensor of the hardware, and ${}^B \mathbf{\Omega} = [p \ q \ r]^T \in \mathbb{R}^{3 \times 1}$ is the body rotation speed of the hardware.

III. CONTROLLER DESIGN

The operation goal of the proposed system is to fly the platform in three-dimensional space without attitudinal motion while loading arbitrary cargo randomly on the upper surface of the platform. Therefore, this section introduces a flight control method with a zero roll and pitch attitude.

For a new platform, an unknown cargo payload causes flight control difficulties. Since the physical properties of the loaded cargo are unknown, the values below are also unknown among the many physical characteristics of the platform:

- The CoM ${}^{B}\mathbf{p}_{c}$ after the payload loading is unknown.
- Mass *m* is unknown.
- Moment of inertia J is unknown.

Among these, unknown m and J affect translational and rotational motion control performance. Still, it is well known that stable flight is possible by using a robust controller against these uncertainties [19]. However, the unknown ${}^{B}\mathbf{p}_{c}$ value leads to uncertainty in wrench generation, especially the ${}^{B}\mathbf{T}$ in Equation (1), which is the most fundamental of system control. Therefore, to transport the unknown payload safely, estimating ${}^{B}\mathbf{p}_{c}$ is essential to prevent unstable and unsatisfactory flight performance. In this section, we first introduce the control allocation method for our unique flight mechanism and then introduce the MOCE algorithm, a dedicated model-free online ${}^{B}\mathbf{p}_{c}$ estimation technique for stable 6-DOF flight control.

A. Control allocation

The new platform has two types of actuators: propeller thrusters and servomotors. Let us define $\mathbf{C} = [\mathbf{C}_1^T \ \mathbf{C}_2^T]^T \in \mathbb{R}^{6\times 1}$, where $\mathbf{C}_1 = [F_1 \ F_2 \ F_3 \ F_4]^T$ is a thruster command and $\mathbf{C}_2 = [\theta_1 \ \theta_2]^T$ is a servomotor command. We can then rewrite Equation (1) as Equation (5). Here, $M_\tau \in \mathbb{R}^{3\times 4}$ is a mapping matrix between \mathbf{C}_1 and ${}^B\mathbf{T}$. Parameters r and l represents arm length and servo motor dimension, respectively, as shown in Fig. 1. However, M_τ includes the $\theta_{\{1,2\}}$ component, which is a component of \mathbf{C}_2 , in a manner of multiplicative and transcendental function to other physical properties and states. Similarly, Equation (3) shows that both \mathbf{C}_1 and \mathbf{C}_2 are also used simultaneously to generate a desired ${}^B\mathbf{F}$ value. Since \mathbf{C}_1 and \mathbf{C}_2 are intricate in making ${}^B\mathbf{W}$, we cannot allocate the actuator control input through a simple conventional mapping matrix inverse or pseudo-inverse methods [20].

To overcome this, we devised a sequential two-step method by utilizing the characteristics of heterogeneous actuators; the propulsion motor control response is significantly faster than the angle control response of the servomotor. 1) Step 1: The first step of sequential control allocation is to calculate thruster commands (i.e. $C_{1,cmd}$) to achieve the desired ${}^{B}\mathbf{T}$ and F_{z} values among the components of the wrench ${}^{B}\mathbf{W}$ in the same way as a conventional multirotor control. From Equations (3) and (5), the relationship between the selected states of ${}^{B}\mathbf{W}$ and $C_{1,cmd}$ are as follows:

$$\mathbf{C}_{1,cmd} = M^{-1} \begin{pmatrix} {}^{B}\mathbf{p}_{c}, \mathbf{C}_{2} \end{pmatrix} \begin{bmatrix} {}^{B}\mathbf{T} \\ {}^{F}_{z} \end{bmatrix}_{des},$$
(6)

where

$$M({}^{B}\mathbf{p}_{c},\mathbf{C}_{2}) = \begin{bmatrix} M_{\tau}({}^{B}\mathbf{p}_{c},\mathbf{C}_{2}) \\ -c\theta_{1} & -c\theta_{2} & -c\theta_{1} & -c\theta_{2} \end{bmatrix} \in \mathbb{R}^{4 \times 4}.$$
(7)

Here, $\theta_{\{1,2\}}$ constantly changes during translational motion control, which will be described in the sequel. The M^{-1} matrix requires an update of $\theta_{\{1,2\}}$ in every control iteration. However, since the response of the propulsion motor is significantly faster than that of the servo motor, we can treat the M matrix as a static map in the specific step of the control iteration.

2) Step 2: Once $C_{1,cmd}$ is obtained through Equation (6) in Step 1, we aquire the $F_{A\{1,2\},cmd}$ value. Then, from Equation (3), $C_{2,cmd}$ can be calculated as follows:

$$\mathbf{C}_{2,cmd} = \begin{bmatrix} asin\left(\frac{F_{y,des}}{F_{A1,cmd}}\right)\\ asin\left(\frac{F_{x,des}}{-F_{A2,cmd}}\right) \end{bmatrix}.$$
 (8)

Once the $C_{2,cmd}$ is calculated, we then update the servo angles inside the M^{-1} matrix of Step 1 by using the actual C_2 signal passed through the dynamic model of the servomotor. However, if the actual angle of the servomotor can be measured directly, this measurement can be used instead of the servomotor dynamics model.

Through the proposed sequential method, we can compute the C_{cmd} signal for generating ${}^{B}W$. The overall sequential control allocation method is summarized in Fig. 2. Next, we discuss a technique for estimating changes in the ${}^{B}\mathbf{p}_{c}$ value due to unspecified cargo loading.

B. MOCE algorithm

Let us define ${}^{B}\mathbf{p}_{c} = {}^{B}\hat{\mathbf{p}}_{c} + \Delta\mathbf{p}_{c}$, where $(\hat{*})$ denotes the estimated value and $\Delta\mathbf{p}_{c} = [\Delta x_{c} \ \Delta y_{c} \ \Delta z_{c}]^{T}$ represents the error. We can then rearrange Equation (5) as follows:

$${}^{B}\mathbf{T} = {}^{B}\bar{\mathbf{T}} + {}^{B}\Delta\mathbf{T}, \begin{cases} {}^{B}\mathbf{T} = M_{\tau}({}^{B}\hat{\mathbf{p}}_{c}, \mathbf{C}_{2})\mathbf{C}_{1} \\ {}^{B}\Delta\mathbf{T} = -\Delta\mathbf{p}_{c\times}{}^{B}\mathbf{F} \end{cases}, \quad (9)$$

where ${}^{B}\bar{\mathbf{T}}$ is a nominal (or desired) torque and ${}^{B}\Delta\mathbf{T}$ is an uncertainty-driven undesired torque. From this equation, we can see that $\Delta \mathbf{p}_{c}$ causes ${}^{B}\Delta\mathbf{T}$ generation during translational motion controlled by ${}^{B}\mathbf{F}$.

Generation of the undesired torque is a widespread phenomenon in most UAV control, and many solutions [19], [21]–[23], such as integrator control of the PID controllers, high-gain control or the robust control techniques are widely utilized to compensate for static and dynamic uncertainties. However, in our case, undesired torque is generated by ${}^{B}\mathbf{F}$, which is for translational motion control and changes dynamically. It also has a relatively wide bandwidth to match the needs of a high-level translational motion controller. For the dynamic uncertainty compensation of the ${}^{B}\mathbf{T}$ signal, a robust control method such as "Disturbance Observer (DOB)" controller [19] may be a tempting option; however, in the case of DOB application in actual UAV flights, the bandwidth of the disturbance that can cope with is limited due to the fuselage vibration and sensor noises. Thus, it is not suitable as a solution in our case.

Instead, we can think of estimating the accurate ${}^{B}\mathbf{p}_{c}$ value online during the flight after the unknown cargo is loaded; the ${}^{B}\Delta\mathbf{T}$ can then be removed systematically since $\Delta\mathbf{p}_{c}$ converges to zero. For the estimation of ${}^{B}\mathbf{p}_{c}$, we adopted the concept of the "ESC" technique. ESC is a model-free control technique to find a local minimizer of a given time-varying cost function by applying a persistently exciting periodic perturbation to a set of chosen inputs and monitoring the corresponding output changes [24], [25]. The ESC concept was chosen for CoM estimation because it is model-free; the model-free method matches our system since the control allocation technique is non-linear and the physical properties of the cargo-loaded vehicle are unknown.

The basic operation principle of the ESC algorithm is to periodically perturb some of the state variables of the platform, which is already controlled by high-level controllers, and process the perturb-induced measurements to find the gradient of a cost function to optimize the cost. Three systems are mostly operating at the same time, and it is well known that for guaranteed system performance, the time scales must be clearly distinguishable as follows [18]:

- Fast plant with the (stabilizing) high-level controller,
- Medium periodic perturbation,
- Slow optimization algorithm.

Therefore, in our design, we also clearly distinguish the time scales of the system.

A block diagram of the proposed MOCE algorithm is shown in Fig. 3. First, the control wrench ^BW signal is generated by the "High-level controllers", which are the set of cascaded controllers managing the vehicle pose control. The highlevel controllers operate the three-dimensional translational acceleration to follow target position and velocity commands while simultaneously aiming to maintain zero roll and pitch attitude. Among the wrench signals, a dither signal d is added to ^BF to get the input ^BF̃ (= ^BF + d) to the system, where $d = [d_1 d_1 d_2]^T \in \mathbb{R}^{3\times 1}$ and $d_1 = a_1 \sin \omega_1 t, d_2 = a_2 \sin \omega_2 t$. We make the following assumptions in our stability proof of this system.

Assumption 1: The dither signal d has a relatively small amplitude and does not harm the stability of the entire system

$${}^{B}\mathbf{T} = M_{\tau} ({}^{B}\mathbf{p}_{c}, \mathbf{C}_{2})\mathbf{C}_{1} = \begin{bmatrix} -(l-z_{c})s\theta_{1} + y_{c}c\theta_{1} & (r+y_{c})c\theta_{2} + \xi s\theta_{2} & -(l-z_{c})s\theta_{1} + y_{c}c\theta_{1} & -(r-y_{c})c\theta_{2} + \xi s\theta_{2} \\ (r-x_{c})c\theta_{1} + \xi s\theta_{1} & (l+z_{c})s\theta_{2} - x_{c}c\theta_{2} & -(r+x_{c})c\theta_{1} + \xi s\theta_{1} & (l+z_{c})s\theta_{2} - x_{c}c\theta_{2} \\ (r-x_{c})s\theta_{1} - \xi c\theta_{1} & -(r+y_{c})s\theta_{2} + \xi c\theta_{2} & -(r+x_{c})s\theta_{1} - \xi c\theta_{1} & (r-y_{c})s\theta_{2} + \xi c\theta_{2} \end{bmatrix} \begin{bmatrix} F_{1} \\ F_{2} \\ F_{3} \\ F_{4} \end{bmatrix}$$
(5)



Fig. 2. Structure of the proposed sequential control allocation method considering heterogeneous actuator characteristics and system nonlinearity. The proposed structure uses real-time updates of the *M* matrix by utilizing servomotor angle C_2 information and generates a thruster command $C_{1,cmd}$ for attitude control. Once $C_{1,cmd}$ is determined, the servomotor command for achieving target motion is generated by substituting the corresponding information and target translational force ${}^BF_{\{x,y\},des}$ into Equation (8).

controlled by the high-level controller.

Here, we set ω_1 and ω_2 far enough apart and also distinguish them from the major frequency band of the ${}^B\mathbf{F}$ signal. Then, due to the **d** signal, the vehicle shows an oscillatory translation in all the *x*, *y*, and *z* directions while simultaneously vibrating in the roll, pitch, and yaw attitudinal directions due to the ${}^B\Delta\mathbf{T}$ of Equation (9) when ${}^B\mathbf{p}_c$ is yet correctly estimated.

Next, we estimate the resultant attitude control torque $({}^{B}\mathbf{T})$ by the " $\hat{J}s$ " block, which is a simple differentiator with an estimated MoI tensor multiplied. The gyroscopic effect of the airframe is small that it is permissible to neglect the term $\mathbf{\Omega} \times J\mathbf{\Omega}$ in Equation (4). The " $\hat{J}s$ block is situated because the IMU sensor cannot directly measure rotational acceleration. We then compare ${}^{B}\bar{\mathbf{T}} (= {}^{B}\mathbf{T}_{des})$ and ${}^{B}\hat{\mathbf{T}}$ to capture the ${}^{B}\Delta\mathbf{T}$ ($\approx {}^{B}\hat{\mathbf{T}} - {}^{B}\bar{\mathbf{T}}$) signal.

The full extension of the ${}^{B}\Delta \mathbf{T}$ signal in Equation (9) shows the following structure:

$${}^{B}\Delta\mathbf{T} = \begin{bmatrix} \Delta\tau_{x} \\ \Delta\tau_{y} \\ \Delta\tau_{z} \end{bmatrix} = \begin{bmatrix} -\tilde{F}_{z}\Delta y_{c} + \tilde{F}_{y}\Delta z_{c} \\ \tilde{F}_{z}\Delta x_{c} - \tilde{F}_{x}\Delta z_{c} \\ -\tilde{F}_{y}\Delta x_{c} + \tilde{F}_{x}\Delta y_{c} \end{bmatrix}.$$
 (10)

From the equation above, we can see that each element of ${}^{B}\Delta \mathbf{T}$ is a result of a combination of two translational motions in different directions, meaning that the effects of the CoM errors on two directions are indistinguishable. A band-pass filter can be utilized to overcome this issue since the frequencies of d_1 and d_2 of **d** are set to be clearly distinguishable ($\omega_1 \neq \omega_2$).

The proposed estimation process is as follows. First, we rearrange ${}^{B}\Delta \mathbf{T}$ by a mapping function $K : \mathbb{R}^{3 \times 1} \to \mathbb{R}^{3 \times 1}$ using the following equation:

$$\mathbf{K} = K(^{B}\Delta\mathbf{T}) = \begin{bmatrix} k_{1} \\ k_{2} \\ k_{3} \end{bmatrix} = \begin{bmatrix} \Delta\tau_{y} \\ -\Delta\tau_{x} \\ \Delta\tau_{x} \text{ or } -\Delta\tau_{y} \end{bmatrix}.$$
 (11)

Then, we apply a standard second-order band-pass filter $H_{\{1,2\}}(s)$ to the $k_{\{1,2,3\}}$ signal, as shown in Fig. 3 ("Band-pass filter" block), where

$$H_{\{1,2\}}(s) = \frac{\frac{\omega_{\{1,2\}}}{Q_{\{1,2\}}}s}{s^2 + \frac{\omega_{\{1,2\}}}{Q_{\{1,2\}}}s + \omega_{\{1,2\}}^2}$$

 $\omega_{(*)}$ and $Q_{(*)}$ represent the natural frequency and Q-factor, respectively. Next, we make the following assumption regarding the performance of the band-pass filter $H_{\{1,2\}}(s)$.

Assumption 2: If the dither signal $d_{\{1,2\}}$ is set far from the major frequency band of the ^BF signal, and if $\Delta \mathbf{p}_c$ is updated slowly enough, $\omega_{\{1,2\}}$ and $Q_{\{1,2\}}$ exist so that the following equation holds:

$$\tilde{\mathbf{K}} = \begin{bmatrix} \tilde{k}_1 \\ \tilde{k}_2 \\ \tilde{k}_3 \end{bmatrix} = diag(H_2, H_2, H_1) \mathbf{K} \approx \begin{bmatrix} d_2 \Delta x_c \\ d_2 \Delta y_c \\ d_1 \Delta z_c \end{bmatrix} .$$
(12)

Here, the $H_{\{1,2\}}$ block filters out the translational motion control signal (= ${}^{B}\mathbf{F}$) from ${}^{B}\tilde{\mathbf{F}}$ and outputs only the dither signal with the specific frequency (= $d_{\{1,2\}}$), where ${}^{B}\tilde{\mathbf{F}} =$ ${}^{B}\mathbf{F} + \mathbf{d}$. With this assumption, we can extract the $\Delta \mathbf{p}_{c}$ signals multiplied by the artificial dither signal among the components of the ${}^{B}\Delta\mathbf{T}$ signal in Equation (10). Through the demodulation process shown in Fig. 3, we can extract the signal with the square of the dither signal for each channel ($\gamma_{1}, \gamma_{2}, \gamma_{3}$) where

$$\boldsymbol{\Gamma} = \begin{bmatrix} \gamma_1 \\ \gamma_2 \\ \gamma_3 \end{bmatrix} = \begin{bmatrix} d_2^2 \Delta x_c \\ d_2^2 \Delta y_c \\ d_1^2 \Delta z_c \end{bmatrix}, \quad (13)$$

and can find a gradient for making $\Delta \mathbf{p}_c \rightarrow 0$.

The remainder of the process is as follows. In each channel, if the current estimate of the $\Delta \mathbf{p}_c$ element is positive, then the $\gamma_{(*)}$ signal will also be positive since the two sinusoidal signals $(k_{(*)})$ and demodulation signal $d_{(*)})$ are in phase. Similarly, the $\gamma_{(*)}$ signal will be negative if the $\Delta \mathbf{p}_c$ element is negative since the two sinusoidal signals are out of phase. In either case, the product of the two sinusoids will have a "DC component", which is extracted by the low-pass filter to become the $\mathbf{V} = [v_1 \ v_2 \ v_3]^T$ signal. Then, by integrating \mathbf{V} signals with proper tunable gains $-g_{(*)} \in \mathbb{R} \leq 0$ for update speed control, which must be a small gain due to the time scale separation, we can estimate the CoM values and converge $\Delta \mathbf{p}_c$ to zero [18].

C. Stability

Since the MOCE algorithm has the same structure for all channels, the stability of the algorithm is examined by picking the x channel (x_c estimation). The estimation process is comprised of four steps: band-pass filter, demodulation, low-pass filter, and integrator, as shown in Fig. 3. However, the band-pass filtering and demodulation process must be configured to satisfy Assumptions 1 and 2. Therefore, we investigated the conditions of the low-pass filter and integrator to achieve the stability of the overall estimation process.

From Equations (10) through (12) and Fig. 3, we can see that the update of x_c is made from the $\Delta \tau_y$ signal that has passed through the $H_2(s)$ filter. We can then simplify the x_c estimation process, as shown in Fig. 4-(a). In addition, with the satisfactory operation of the $H_2(s)$ filter based on Assumption 2, we can further simplify the diagram, as shown in Fig. 4-(b).

Summarizing the system 4-(b) gives the following results,

$$\frac{d}{dt} \begin{bmatrix} \Delta x_c \\ v_1 \end{bmatrix} = \begin{bmatrix} -g_2 v_1 \\ -\omega_{\{L,2\}} v_1 + \omega_{\{L,2\}} \gamma_1 \end{bmatrix}, \quad (14)$$



Fig. 3. Block diagram of the proposed flight controller with MOCE algorithm during flight.



Fig. 4. (a) Block diagram of x-axial CoM estimation process. (b) Simplified block diagram with an application of Assumption 2.

where the low-pass filter is set to have $L_2(s) = \omega_{\{L,2\}}/(s + \omega_{\{L,2\}})$. Our goal is to find g_2 and $\omega_{\{L,2\}}$ that ensure system stability in Equation (14). To analyze system stability, the averaging method is utilized [18]. First, let us define

$$\tau = \omega_2 t$$

$$g_2 = \omega_2 \delta g'_2 = O(\omega_2 \delta) , \qquad (15)$$

$$\omega_{\{L,2\}} = \omega_2 \delta \omega'_{\{L,2\}} = O(\omega_2 \delta)$$

where δ is a small positive constant and g'_2 and $\omega'_{\{L,2\}}$ are O(1) positive constants. Then, Equation (14) becomes as follows:

$$\frac{d}{d\tau} \begin{bmatrix} \Delta x_c \\ v_1 \end{bmatrix} = \delta \begin{bmatrix} -g'_2 v_1 \\ -\omega'_{\{L,2\}} v_1 + \omega'_{\{L,2\}} \Delta x_c a_2^2 \left(\sin^2(\tau) \right) \end{bmatrix},\tag{16}$$

where $\gamma_1 = d_2^2 \Delta x_c$ and $d_2 = a_2 \sin \omega_2 t$. If we set g'_2 to be small enough, then we can consider that Δx_c remains nearly constant during a single oscillation of the d_2 signal. With this in mind, the average model of Equation (16) becomes as follows:

$$\frac{d}{d\tau} \begin{bmatrix} \Delta x_c^a \\ v_1^a \end{bmatrix} = \delta \begin{bmatrix} -g_2' v_1^a \\ -\omega_{\{L,2\}}' v_1^a + \frac{\omega_{\{L,2\}}' \Delta x_c^a a_2^2}{2\pi} \int_0^{2\pi} \sin^2 \tau d\tau \end{bmatrix},$$
(17)

which finally becomes

$$\frac{d}{d\tau} \begin{bmatrix} \Delta x_c^a \\ v_1^a \end{bmatrix} = \delta B \begin{bmatrix} \Delta x_c^a \\ v_1^a \end{bmatrix}, \ B = \begin{bmatrix} 0 & -g_2' \\ 0.5\omega'_{\{L,2\}}a_2^2 & -\omega'_{\{L,2\}} \end{bmatrix},$$
(18)

TABLE I PARAMETERS AND CONTROLLER GAINS

Hardware Parameter	Value	Hardware Parameter	Value
${m \over r}$	2.405 Kg	<i>l</i>	0.015 m
	0.109 m	ξ	0.01
Estimator Parameter	Value	Controller Gain	Value
$egin{array}{llllllllllllllllllllllllllllllllllll$	0.3, 0.7	P (Roll, Pitch)	2.0
	5, 3 rad/s	D (Roll, Pitch)	0.45
	1.5, 0.5	P (X, Y Position)	2.0
	20	I (X, Y Position)	0.5
	0.5 rad/s	D (X, Y Position)	0.7

where $(*)^a$ represents the average value over a single period of oscillation. Then, the *B* matrix will be Hurwitz if

$$g'_2, \ \omega'_{\{L,2\}} > 0$$

and the CoM estimation process becomes stable with these inequality conditions. However, based on the averaging analysis [26], the δ value must be kept small, indicating that both g_2 and $\omega_{\{L,2\}}$ in Equation (15) must also be small.

The same principle applies to the Δy_c and Δz_c estimation channels, meaning that the overall conditions for the stability of online CoM estimation become

$$0 < \omega_{\{L,\{1,2\}\}}, \ 0 < g_{\{1,2\}}$$

and those parameters must maintain a small value to achieve system stability.

IV. EXPERIMENT

Experiments with two different flight scenarios were conducted to validate the performance of the MOCE algorithm and the capability of stably transporting an unknown payload. Table 1 shows the proposed vehicle's physical and control parameters.¹

A. CoM estimation performance

The first experiment was conducted to validate the performance of the MOCE algorithm. As shown in Fig. 5-(a), in this scenario, the weight with a known mass (0.2 Kg) is attached at a specific position $([0.184 \ 0 \ -0.121]^T \ \text{m}$ in the body frame); thus, the actual CoM of the entire system is known

¹An experiment video can be found at https://youtu.be/g5yMb22a8Jo.



Fig. 5. Experiment environment for performance validation. (a) Experiment to estimate the position of the changed CoM after attaching a weight to a fixed position. (b) Flight experiment in which a constant attitude is not maintained during translational motion due to ill-estimated CoM when the proposed MOCE algorithm is turned off. (c) Flight experiment maintaining a constant attitude incorporating the proposed MOCE algorithm with updated CoM.



Fig. 6. Flight data of the proposed CoM localization algorithm. (Left three columns) The states of the platform vibrate due to the dither signal. The blue dotted line is the desired value, and the solid orange line is the sensor data. (Middle column) Γ and \mathbf{V} vector signals that change over time during the CoM estimation process. (Right column) Vector of CoM estimates that change over time. The dotted orange line is the true CoM.

 $({}^{B}\mathbf{p}_{c} = [0.0175 \ 0.0085 \ -0.0430]^{T} \text{m})$, derived from the CAD design tool. The CoM estimation algorithm is then activated to validate the performance of the algorithm.

Fig. 6 shows the flight result. The left three columns of the figure show fuselage's roll and pitch attitude, horizontal positions, and two servo angles, respectively. The high-level controller attempts to maintain zero roll and pitch attitude and zero x and y positions. However, due to the dither signal d, an undesired attitude-control torque ${}^{B}\Delta T$ is generated, and the attitude oscillates. Here, the position of the platform remains at zero due to the robustness of the high-level position controller.

The middle and right columns of the figure show the internal process of the MOCE algorithm. In the middle column graphs ("MOCE Process Data" graphs), the blue signals are Γ signals, and the orange signals are V signals, which are low-pass filtered signals. The V signal acts as a gradient of the estimator, where the negative and positive values indicate that the estimated CoM must increase or decrease. In the end, as we see in the graphs on the right column ("Center of Mass Estimation" graphs), the estimation algorithm successfully estimates the actual CoM.

B. Flight experiment carrying an unknown payload

The second experiment is actual payload transportation. In this case, a payload with unknown physical properties is loaded on the platform. Two flight scenarios are conducted to validate the performance of the proposed algorithm. In both scenarios, a position control command making the platform reciprocate about three meters in the *y*-direction is applied. Also, the desired roll and pitch attitude are set to zero in both scenarios.

1) Scenario 1: Fig. 7 shows the flight without the MOCE algorithm. From around 65 seconds, the *y*-directional translational motion begins. At this time, undesired roll and pitch motions occur due to undesired torque. The sequential image of the experiment is shown in Fig. 5-(b).

Failure to maintain the attitude of the platform results in severe impairment of translational motion control. As can be seen in the "Servo Angle" graphs, the rotation of each servomotor is limited to ± 0.3 rad due to hardware limitations. Because of this, the platform can no longer generate the necessary global horizontal thrust force since the fuselage has been severely tilted. Ultimately, the platform collided with the environment at approximately 75 seconds and crashed.

2) Scenario 2: Conversely, Fig. 8 shows the flight with the estimated CoM. Since the CoM is updated, the undesired torque generation is minimized; therefore, the platform can maintain near-zero roll and pitch attitude during the flight. The translational motion performance is also satisfactory due to the thrust control by the two servo motors. The sequential image of the experiment is shown in Fig. 5-(c).²

²The additional flight experiment data can be accessed via the following link. https://drive.google.com/drive/folders/19eqgNmKVR7Y9yJo9PXr8pLj6E1taoRFe?usp=sharing



Fig. 7. Cargo flight results without the MOCE algorithm (blue dashed line: desired value, orange solid line: sensor data). The fuselage attitude is not maintained due to undesired torque generation; as a result, the servo angle reaches the hardware limit, and the overall control fails.



Fig. 8. Cargo flight results with the MOCE algorithm (blue dashed line: desired value, orange solid line: sensor data). The fuselage attitude is maintained within ± 0.05 rad (± 2.86 deg), and the position control is also successful.

V. CONCLUSION

In this research, we introduced a new multirotor UAV platform and a dedicated control method suitable for unknown cargo transportation. To achieve this goal, a platform with a new fully-actuated flight mechanism that can pursue stable cargo transport while maintaining a constant attitude was developed. The platform has a cubic-shaped exterior designed to place unknown cargo anywhere on the flat upper space freely. The MOCE algorithm, a model-free CoM estimation technique inspired by the ESC algorithm, was introduced to overcome the deterioration of the attitude control performance due to undesired torque caused by unknown cargo. For estimation, dither signals having different frequencies are applied to the three-dimensional translational force signal by utilizing the 6-DOF flight performance of the fully-actuated platform. An accurate CoM is then estimated by monitoring the attitudinal vibration. During the estimation process, each roll, pitch, and yaw attitude vibration is caused by three translational dither forces, and a band-pass filter is introduced to distinguish the effect of each dither force in each attitude channel. Finally, the CoM estimation and flight performance were validated through experiments.

The current study is limited in that the estimation process was performed before the translational motion. The requirement of a separate time period for estimation can be a weakness in battery-based aircraft with a limited flight time. Therefore, future research will focus on a technique that can quickly estimate the physical properties while in motion.

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